

# Geometrical Frustration and Quantum Criticality

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# Heavy Fermions: Kondo Lattices

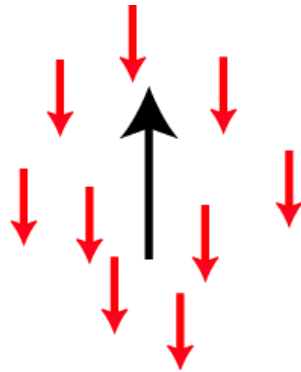


- Exchange Interaction  $J$  generates two competing energy scales

Kondo Effect

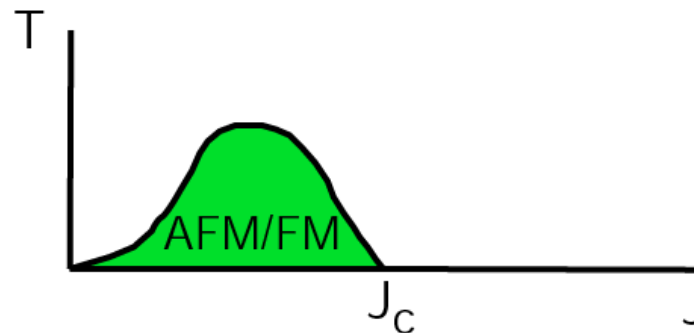
RKKY Interaction

$$T_K \sim \exp(-1/nJ)$$

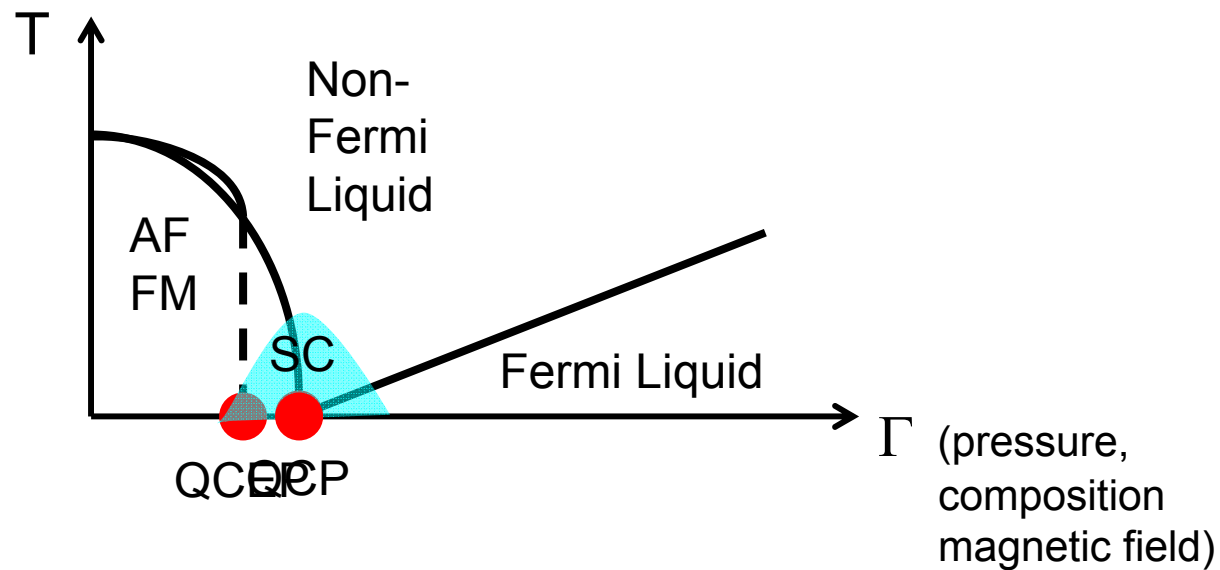


$$T_N \sim J^2$$

- Generic 'Doniach' Phase Diagram:



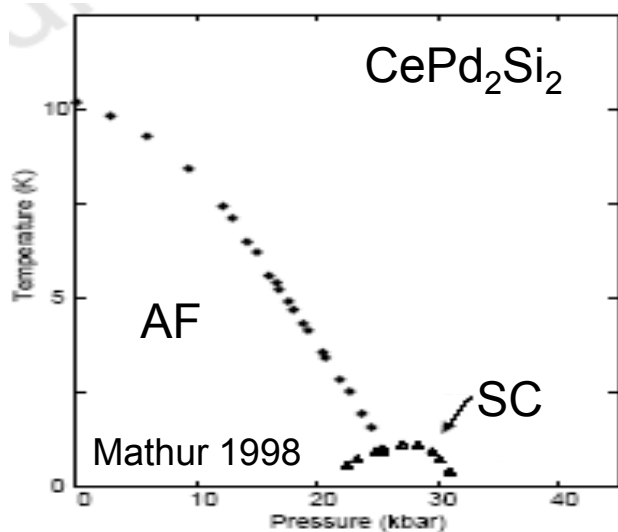
# The Heavy Fermion Phase Diagram



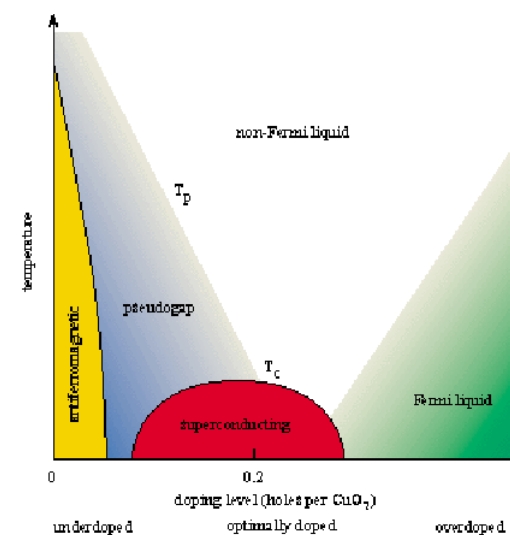
- Disappearance of magnetic order  $T_{N,C} \rightarrow 0$ : unconventional critical phenomena (Quantum Critical Point, Quantum Critical Endpoint).
- Destruction of normal metal  $T_{FL} \rightarrow 0$ : replaced by unconventional metal.
- Collective instabilities of unconventional metals:
  - unconventional superconductivity
  - partial 'nematic' order

# QCPs: Universal Organizing Scheme?

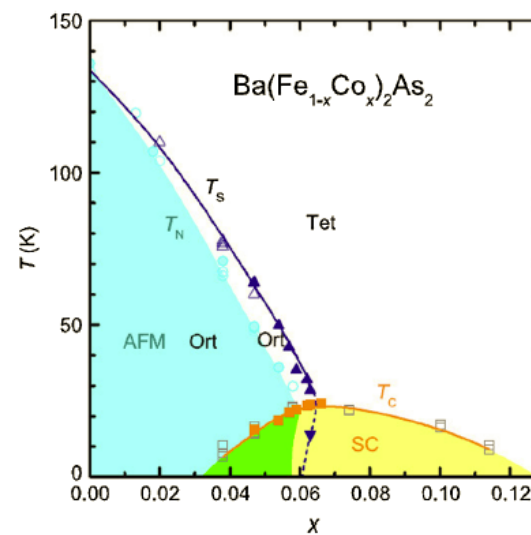
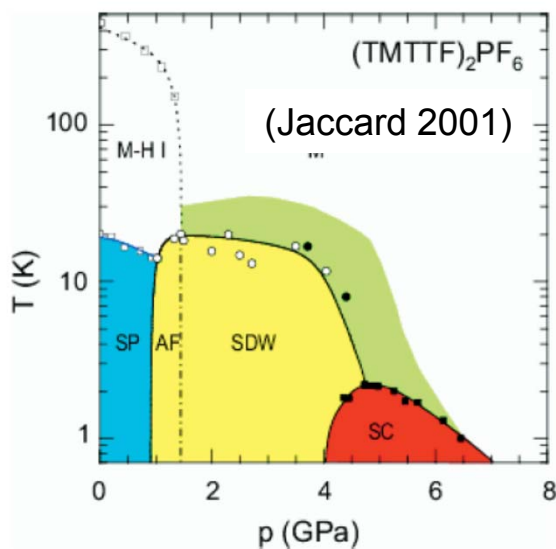
## Heavy Electron Intermetallics



## Cuprates



## Organic Conductors

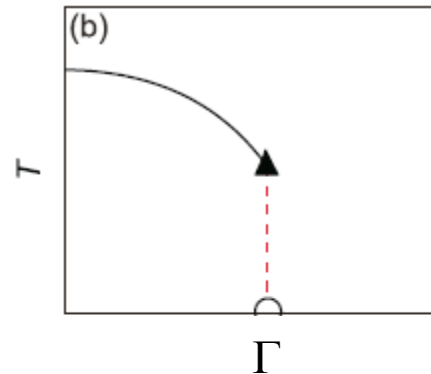
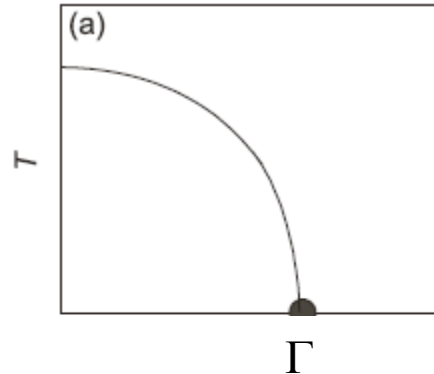


Nandi 2010

# Suppression of Magnetic Order

**Conventional QCP**  
 $T_{N,C} \rightarrow 0$

YbRh<sub>2</sub>Si<sub>2</sub>, CeXIn<sub>5</sub>  
 CeCu<sub>6-x</sub>Au<sub>x</sub>, Cr<sub>1-x</sub>V<sub>x</sub>  
 Ni<sub>1-x</sub>Pd<sub>x</sub>

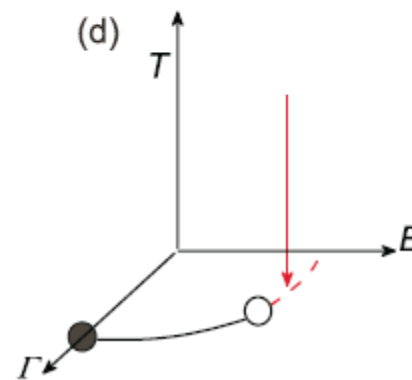
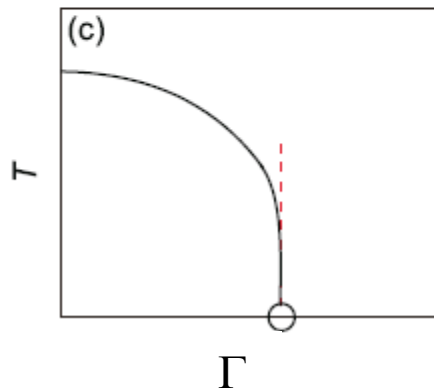


**Tricritical point**  
 $T_C \rightarrow 0$  QCEP

FeCl<sub>2</sub>, MnSi, ZrZn<sub>2</sub>,  
 UGe<sub>2</sub>

**QCEP**  $T_{N,C} = 0$

CeRh<sub>2</sub>Si<sub>2</sub>, Yb<sub>3</sub>Pt<sub>4</sub>  
 CeNiGe<sub>3</sub>, Yb<sub>5</sub>Pt<sub>9</sub>

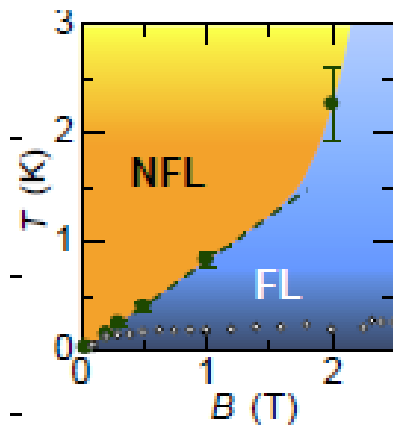


**Metamagnetic**  
 (no phase transition)

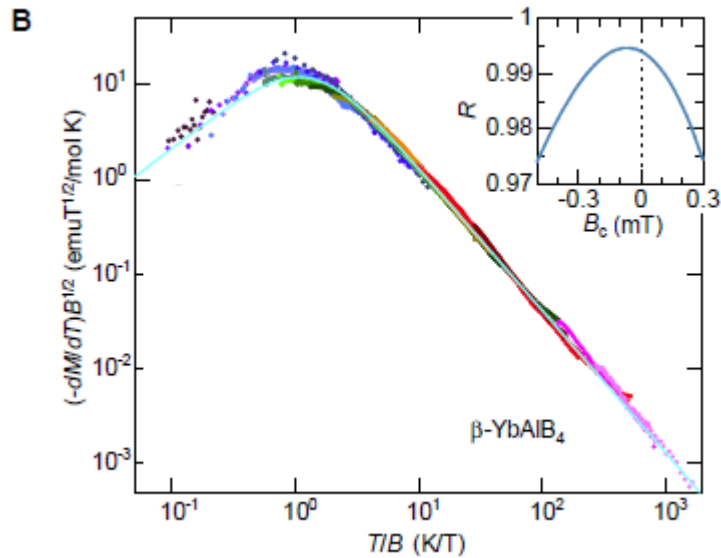
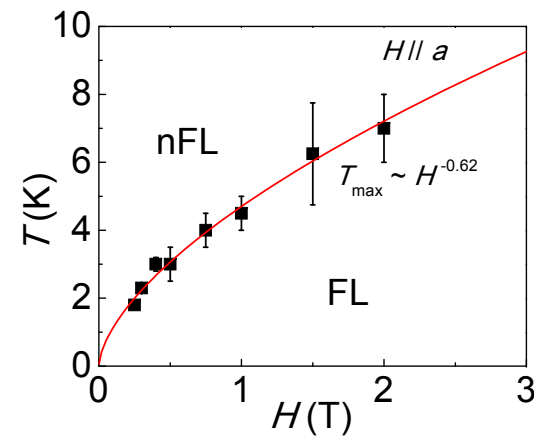
CeRu<sub>2</sub>Si<sub>2</sub>, Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>

# Field-Tuned Quantum Criticality $T_C=0, H=0$

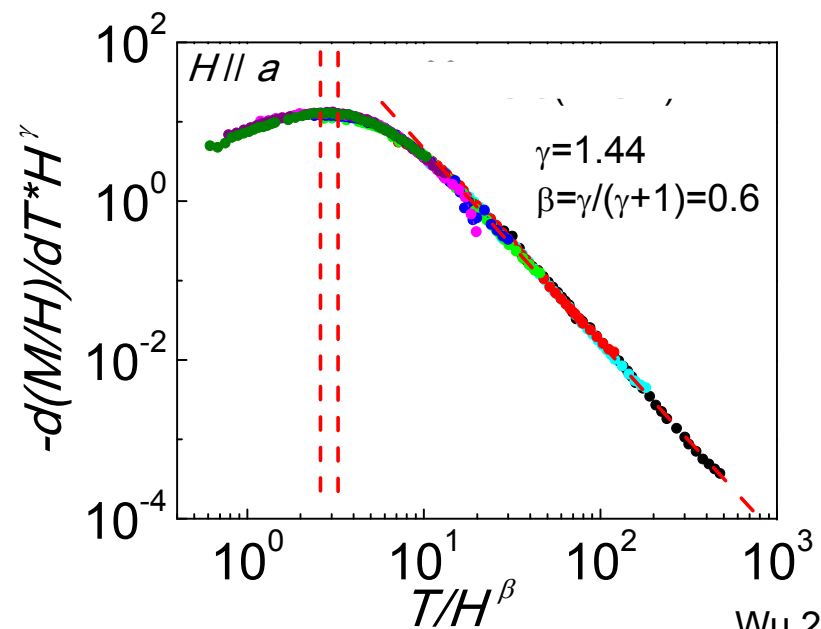
$\beta$ -YbAlB<sub>4</sub>



YFe<sub>2</sub>Al<sub>10</sub>

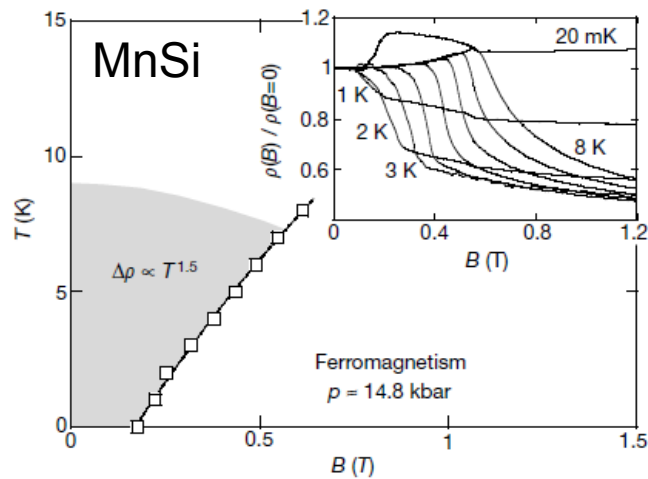
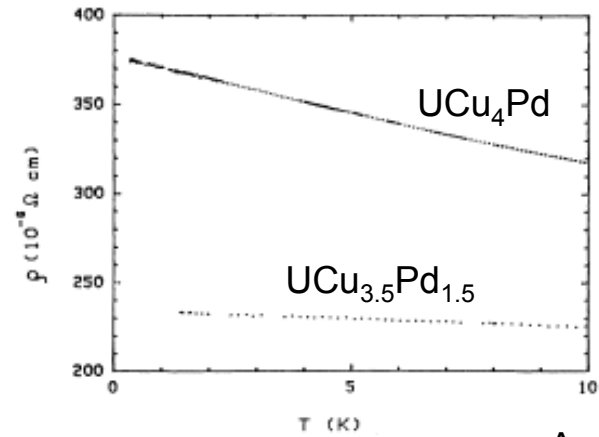
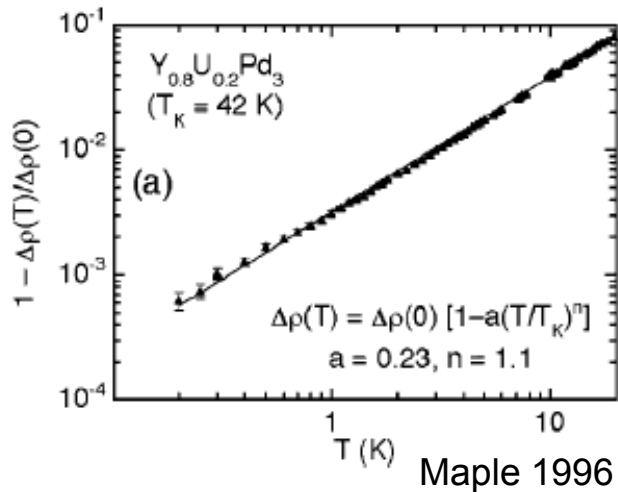


Matsumoto 2011

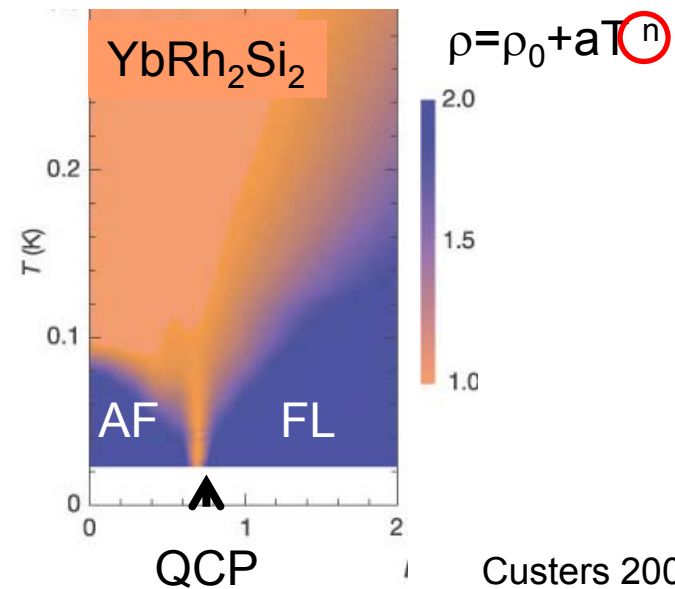


Wu 2012

# Non-Fermi Liquid Metals

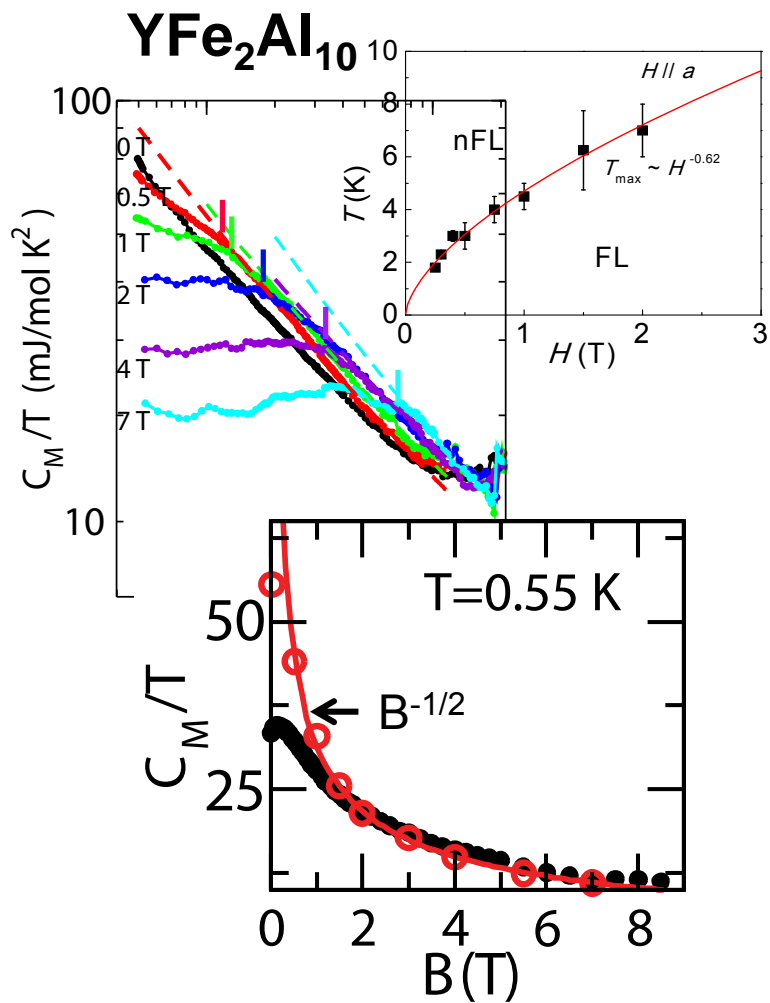
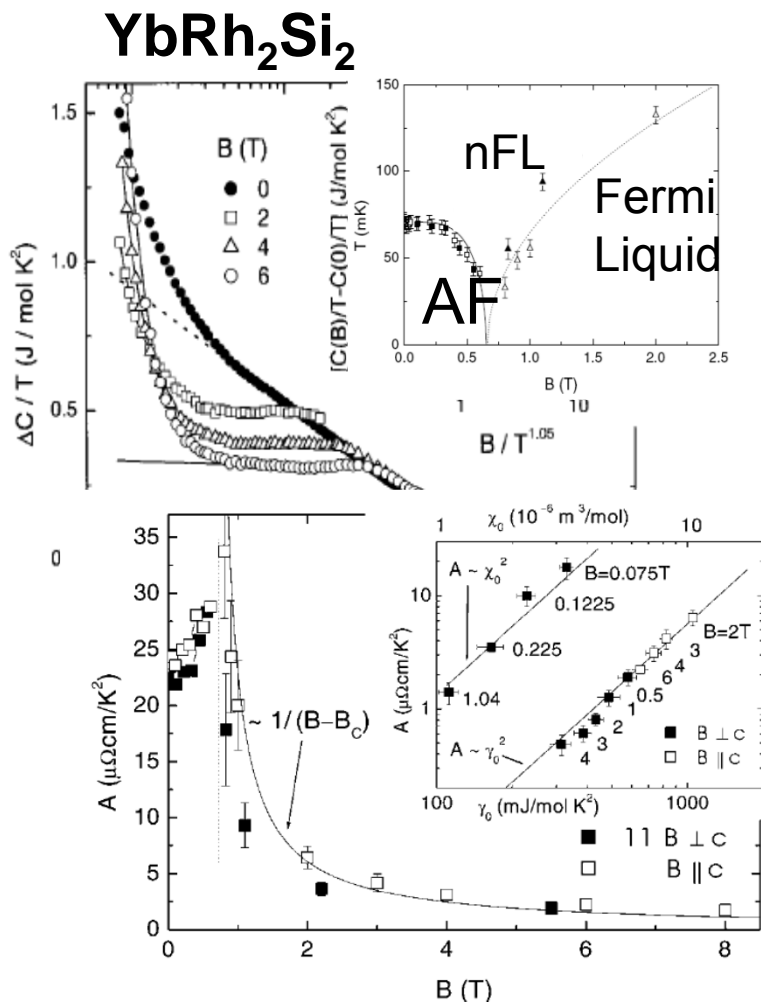


Pfleiderer 2001



Custers 2003

# Breakdown of Fermi Liquid Phase at QCP



- $T_{FL} \rightarrow 0$ : divergence of quasiparticle mass enhancement  $m^*/m$  at QCP

YbRh<sub>2</sub>Si<sub>2</sub> (B=B<sub>QCP</sub>):  $\gamma = 0.65$  J/mol-Yb-K<sup>2</sup>

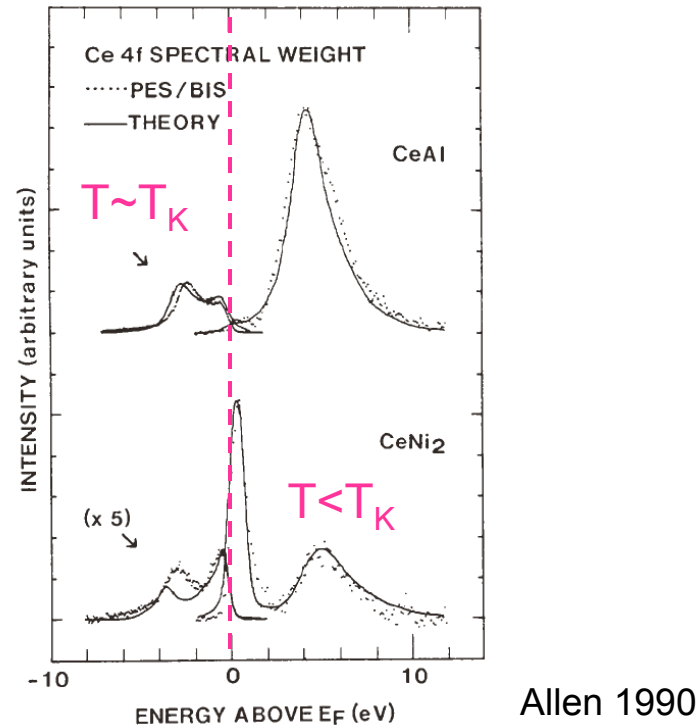
YFe<sub>2</sub>Al<sub>10</sub> (B=0.5 T):  $\gamma \sim 42$  mJ/mol-Fe-K<sup>2</sup>

YbRh<sub>2</sub>Si<sub>2</sub>:  $\gamma(B) \sim (B - B_{QCP})^{-1/2}$

YFe<sub>2</sub>Al<sub>10</sub>:  $\gamma(B) \sim B^{-1/2}$

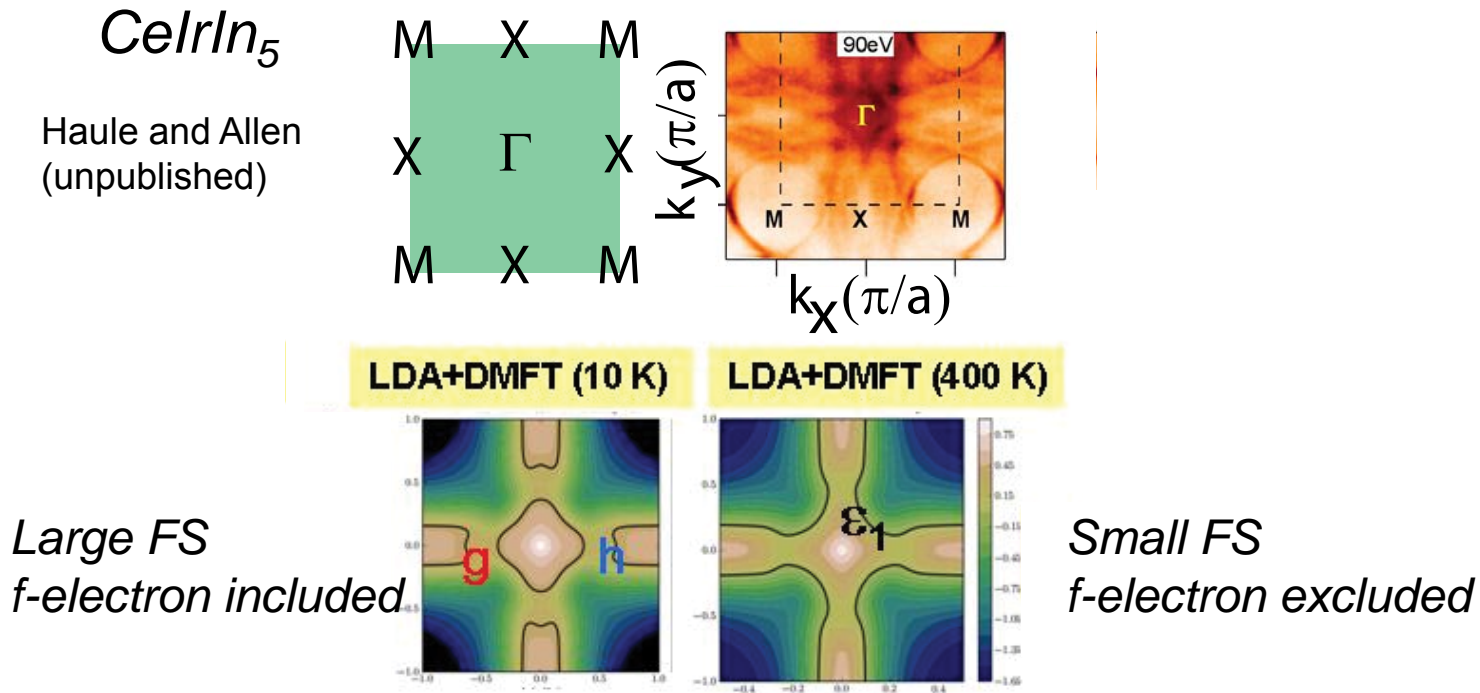


# f-electrons and the Fermi Surface: the Kondo resonance



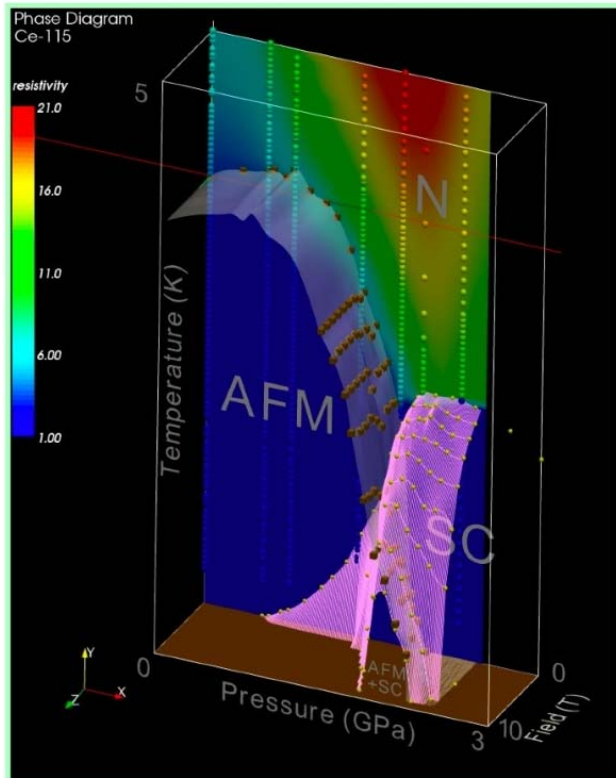
- $T \gg T_K$ : Localized moments decoupled from conduction electrons  
f-electrons excluded from (small) Fermi surface
- $T \ll T_K$ : Formation of Kondo singlet  
f-electrons included in (large) Fermi surface

# Kondo Coherence and the Fermi Surface Volume

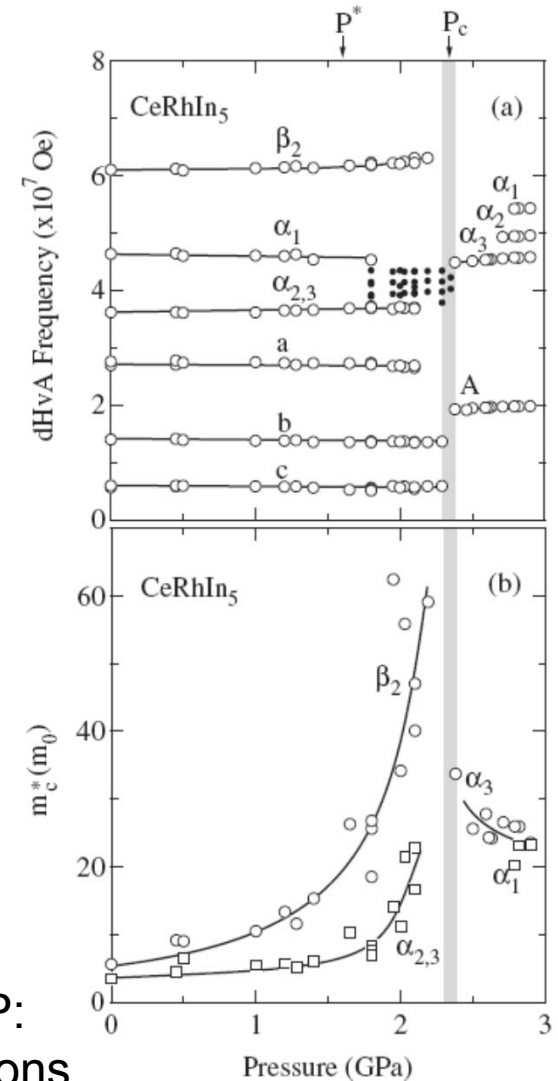
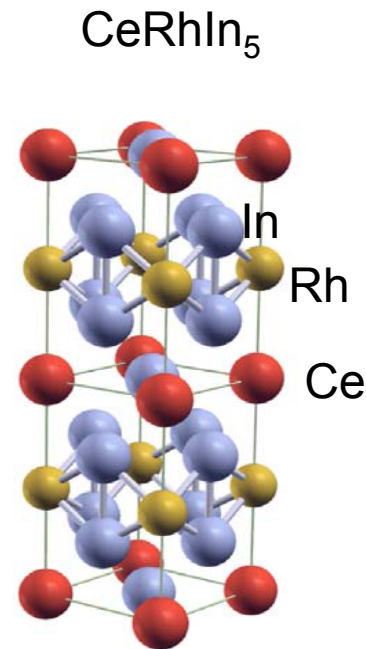


- Does the Fermi surface expand in Kondo lattice systems when the renormalized bands form on cooling?
- T=26 K: Fermi surface of CeIrIn<sub>5</sub> resembles 400 K LDA+DMFT calculation  
f-electron is localized, excluded from (small) Fermi surface.
- Comparison of ARPES and LDA+DMFT well suited to detecting electron delocalization transitions.

# T=0 Electronic Delocalization and the QCP



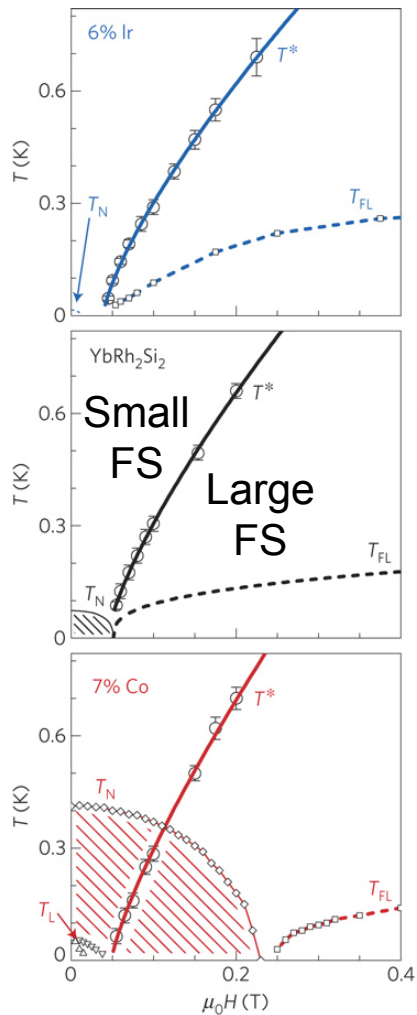
Data: Tuson Park  
Figure rendition: Mathias Graf



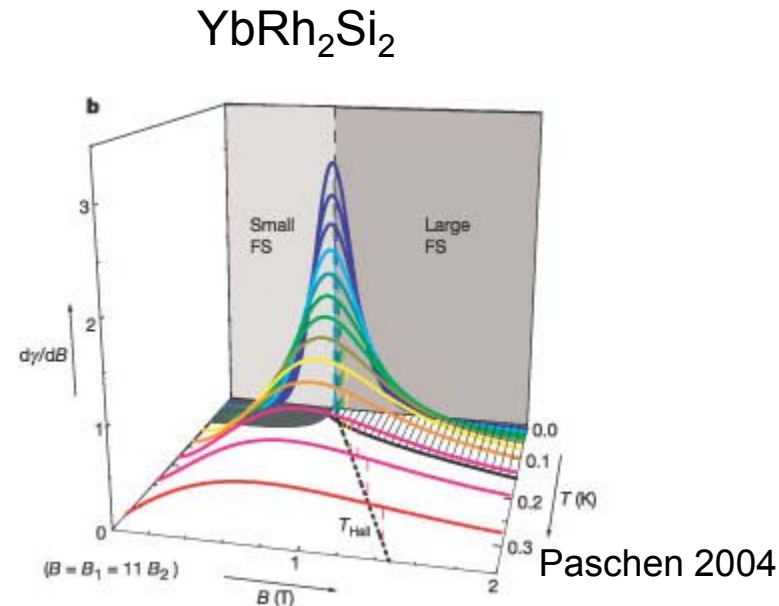
- de Haas- van Alphen measurements at  $P_c=2.3$  GPa QCP:  
Discontinuous change in Fermi surface dimensions  
Divergence of quasiparticle mass
- Superconductivity near  $P_c$ .

(Shishido 2005)

# Electronic Delocalization detached from the QCP

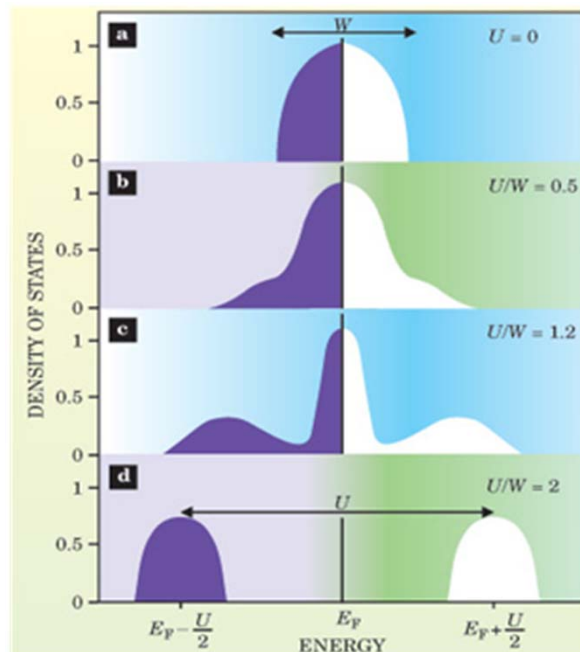


Friedemann 2009

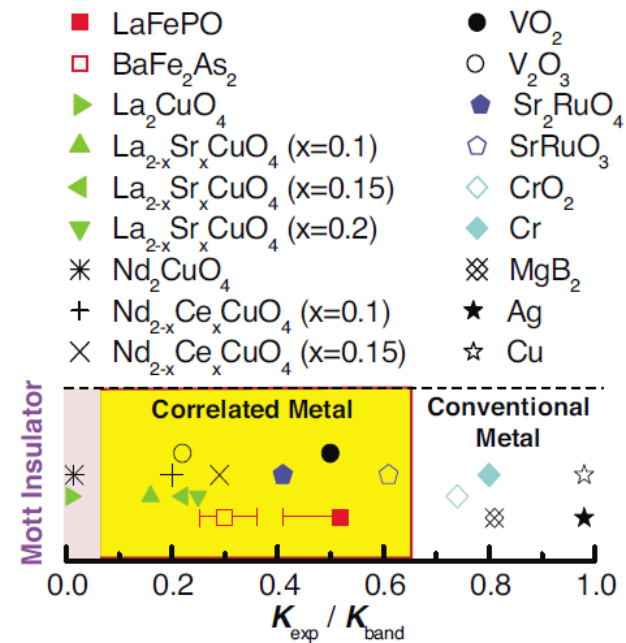


- $T=0$ : Jump in Fermi surface volume (small FS to large FS) for  $H=H^*$
- Since  $T \ll T_K \approx 25$  K, analogous to  $T=0$  Mott transition?

# A General Description of Electronic Delocalization?



Kotliar and Vollhardt 2004



Qazilbash 2009

- Heavy fermion delocalization:
  - metal-metal transition: weaker correlations than oxides
  - larger mass enhancement (small  $K_{\text{exp}}/K_{\text{band}}$ )
- Still needed: a non-Kondo metal with localized moments (small FS)



# Two-Step Electronic Delocalization in Pressurized LaMnPO

